

1 **Relative Homoplasy Index: A New Cross-comparable Metric for Quantifying**
2 **Homoplasy in Discrete Character Datasets**

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19 ABSTRACT

20 Homoplasy is among the main hinderances to phylogenetic inference. However, investigating

21 patterns of homoplasy can also improve our understanding of macroevolution, for instance by

22 revealing evolutionary constraints on morphology, or highlighting convergent form-function

23 relationships. Several methods have been proposed to quantify the extent of homoplasy in

24 discrete character matrices, but the consistency index (CI) and retention index (RI) have

25 remained the most widely used for decades, with little recent scrutiny of their function. Here,

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26 we test the performance of CI and RI using simulated and empirical datasets and investigate
27 patterns of homoplasy with different matrix scenarios. In addition, we describe and test a new
28 scaled metric, the relative homoplasy index (RHI), implemented in the R statistical
29 environment. The results suggest that, unlike the RI, the CI does not constitute a direct
30 measure of homoplasy. However, the RI consistently underestimates the extent of homoplasy
31 in phylogenetic character-taxon matrices, particularly in datasets characterised by high levels
32 of homoplasy. By contrast, RHI—the newly proposed metric—outperforms both methods in
33 sensitivity to homoplasy levels, and is scaled between zero and one for comparison of values
34 between different datasets. Using both simulated and empirical phylogenetic datasets, we
35 show that relative levels of homoplasy remain constant with the addition of novel characters,
36 and, in contrast to earlier work, decrease with the addition of taxa. Our results help illuminate
37 the inherent properties of homoplasy in cladistic matrices, opening new potential avenues of
38 research for investigating patterns of homoplasy in macroevolutionary studies.

39

40 Keywords: Homoplasy, discrete characters, phylogenetics, morphology, parsimony

41

42 INTRODUCTION

43 Homoplasy is an inevitable property of discrete character matrices constructed for
44 phylogenetic inference. In cladistic matrices, homoplasy is defined as the independent
45 acquisition of or reversal to the same character state (Lankester 1870; Sanderson and
46 Donoghue 1989), and is often considered a limitation in morphological datasets as it can
47 obscure phylogenetic relationships (Archie 1996). However, with ever-improving methods to
48 infer phylogenetic relationships and the increasing availability of genomic data for extant
49 clades, accurately quantifying the extent of homoplasy in phylogenetic datasets has potential
50 to be useful for informing estimates of evolvability and constraints on morphological

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51 evolution (Sanderson and Donoghue 1989; Wagner 2000; Sidlauskas 2008; Brocklehurst and
52 Benson 2021).

53 Methods to estimate homoplasy received considerable attention in the late 20th
54 century with an extensive body of research exploring parsimony-based metrics with cladistic
55 matrices (summarised in Archie 1996). In recent years, however, few studies have explored
56 patterns of homoplasy in discrete datasets, and the development of new homoplasy estimation
57 methods have lagged behind methodological advances in phylogenetic inference. The two
58 most widely-implemented and easily calculated homoplasy metrics are the parsimony-based
59 consistency index (CI) (Kluge and Farris 1969) and retention index (RI) (Farris 1989). These
60 metrics are implemented in phylogenetic inference programmes such as TNT (Goloboff et al.
61 2008) and the ‘phangorn’ *R* package (Schliep 2011), and have been subject to numerous
62 comparative analyses on their efficacy for detecting homoplasy, and used to explore patterns
63 of homoplasy within discrete character matrices (Sanderson and Donoghue 1989; Meier et al.
64 1991; Archie 1996; Hauser and Boyajian 1997; Sookias 2020; Murphy et al. 2021).

65 However, CI and RI are not cross-comparable methods; that is, they cannot be
66 directly compared across alternative datasets and phylogenetic trees, limiting attempts to
67 infer generalisable conclusions about patterns of homoplasy in phylogenetic datasets. For
68 instance, CI is highly sensitive to variable numbers of taxa (but not characters) in
69 phylogenetic matrices, with a negative relationship detected between CI and the number of
70 taxa included (Sanderson and Donoghue 1989; Hauser and Boyajian 1997; Murphy et al.
71 2021). By contrast, RI represents a more robust metric with respect to matrix dimensions
72 (Hauser and Boyajian 1997; Murphy et al. 2021). Nonetheless, values of RI are not scaled
73 between zero and one; instead, the minimum value (which indicates the maximum amount of
74 homoplasy possible) is an arbitrary value somewhere in that range (Archie 1996). This
75 property arises because RI is calculated using the theoretical maximum treelength for a given

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76 dataset; that is, the number of steps estimated for a matrix when the tree is a complete
77 polytomy (Farris 1989; Archie 1996). Therefore, in any dataset where the tree has more than
78 one resolved node, RI will never be truly scaled between zero and one, rendering values of RI
79 non-comparable between different datasets. To overcome this problematic issue, Archie
80 (1989) developed the homoplasy excess ratio (HER). Unfortunately, however, this method
81 has its own limitations in that it is not applicable to phylogenies inferred under optimality
82 criteria other than maximum parsimony. For instance, phylogenies inferred through Bayesian
83 inference or incorporating topological constraints are not suitable for this method, as HER
84 implements maximum parsimony to infer topologies from randomised versions of character
85 matrices in order to estimate an expected maximum value of homoplasy. Furthermore, HER
86 is particularly time consuming and computationally demanding to calculate, and as such has
87 not seen wide adoption.

88 Towards improving the rigour of systematic investigations of patterns of homoplasy,
89 we present a novel metric, the relative homoplasy index (RHI), for estimating the extent of
90 homoplasy in phylogenetic datasets. The algorithmic basis for RHI is similar to RI, but the
91 resulting metric is consistently scaled between zero and one for empirical datasets, thus
92 facilitating statistically meaningful comparisons across datasets with differing numbers of
93 taxa and characters. We compare RHI to CI and RI using simulated matrices and empirical
94 datasets, and test the sensitivity of each metric to variation in numbers of taxa, characters,
95 and character state transition rates. We also investigate six empirical datasets deriving from
96 four recent studies on bird phylogenetic relationships (Ksepka et al. 2019; Field et al. 2020;
97 Benito et al. 2022; Steell et al. 2023) to explore these patterns of homoplasy in various bird
98 clades, and analyse simulated character matrices based on these empirical topologies to
99 account for systematic bias from random tree generation methods.

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101 MATERIALS & METHODS

102 *Homoplasy Indices*

103 *Consistency index*—The consistency index (CI) is defined as:

$$104 \quad (1) \quad CI = \frac{L_{min}}{L}$$

105 where L represents tree length (the number of steps for a tree with a given matrix, regardless
106 of whether the tree was inferred from that matrix or not) and L_{min} represents the theoretical
107 minimum tree length for a matrix with the same dimensions (i.e., same number of taxa,
108 characters, and proportion of multistate characters) – that is, the length of the tree if there
109 were no homoplasy in the dataset (Kluge and Farris 1969; Farris 1989). L_{min} is calculated by:

$$110 \quad (2) \quad L_{min} = \sum_{i=1}^{n_c} s_i - 1$$

111 where s_i is the number of states for the i^{th} character, and n_c is the total number of characters in
112 the matrix. As L_{min} is necessarily always $\leq L$ by definition, CI is always a value between 0
113 and 1 ($0 < CI \leq 1$; L_{min} cannot equal 0 as long as there is at least one non-invariable character
114 in the matrix). CI is generally interpreted as how well a dataset ‘fits’ a particular tree under
115 the assumption of parsimony (the ‘consistency’; Kluge and Farris 1969). The complement $1 -$
116 CI can then be interpreted as how poorly a dataset fits the tree under consideration.

117

118 *Retention index*—The retention index (RI) is defined as:

$$119 \quad (3) \quad RI = 1 - \frac{H}{H_{max}} = 1 - \frac{L - L_{min}}{L_{max} - L_{min}} = \frac{L_{max} - L}{L_{max} - L_{min}}$$

120 where H represents the total number of extra steps (i.e., steps due to homoplasy; Kluge and
121 Farris 1969; Farris 1989), and can be calculated by subtracting L_{min} from the observed tree
122 length L ; L_{max} represents the theoretical maximum tree length for the matrix, which is the tree
123 length when the matrix is applied to a completely unresolved tree (star tree or single
124 polytomy) (Farris 1989; Archie 1996; Cuthill et al. 2010).

125 CI and RI can be expressed with respect to each other:

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126 (4) $CI = \frac{L_{min}}{L_{max} - RI(L_{max} - L_{min})}$

127 (5) $RI = \frac{(CI * L_{max}) - L_{min}}{CI * (L_{max} - L_{min})}$

128 From these equations, it follows that RI is equal to 0 when $CI = L_{min}/L_{max}$, i.e., when $L =$
129 L_{max} .

130

131 *Relative homoplasy index*—We introduce a novel metric, the relative homoplasy
132 index (RHI), which is defined as follows:

133 (6) $RHI = \frac{L - L_{min}}{L_{null} - L_{min}}$

134 where L_{null} (null tree length) represents the tree length for the matrix when no phylogenetic
135 signal is present except that which is present due to chance. L_{null} is calculated by taking the
136 median tree length for the empirical matrix with a set of randomised trees. In these
137 randomised trees (null trees), the topology of the empirical tree (i.e., tree shape) is
138 maintained, but the tip names are randomised. Therefore, the properties of the empirical
139 tree—such as number of supported nodes, tree balance, and tree shape—are retained in the
140 set of null trees, avoiding systematic biases associated with these properties (Felsenstein
141 2004; Simmons et al. 2004).

142 The relative homoplasy index differs from the consistency index and retention index
143 in that 0 indicates an absence of homoplasy for a matrix (when $L = L_{min}$), and 1 indicates that
144 a matrix shows as much homoplasy as possible when the corresponding topology is resolved
145 beyond a polytomy (when $L = L_{null}$). In this case, a value of 1 would occur if the matrix
146 contains no phylogenetic information with respect to the tree, beyond that which is present by
147 chance. RHI can be calculated for any discrete matrix with a given phylogeny, regardless of
148 the method or dataset that the phylogeny was inferred from. RHI is a cross-comparable
149 metric that can be applied to matrices with accompanying phylogenetic trees that may have

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150 been generated from independent matrices (e.g., molecular data), when the topology is a
151 consensus between multiple datasets, or when the topology is partially constrained by another
152 phylogenetic hypothesis.

153

154 *Data Acquisition and Analyses*

155 We selected published phylogenetic datasets with a focus on birds to investigate
156 homoplasy in this study. Datasets were selected based on their properties such as tree
157 inference method, taxon and character dimensions, and availability of data from public
158 repositories. The six datasets used in this study are summarised in Table 1 and were taken
159 from four published studies with morphological matrices of different bird taxa. Datasets from
160 Benito et al. (2022) and Steell et al. (2023) were formatted so that two different treatments of
161 the matrix and/or empirical tree could be analysed. For Benito et al., two datasets were
162 analysed (*Avialae a* and *Avialae b*). Both matrices are the same, but the topologies are based
163 on different phylogenetic inference methods; the topology for *Avialae a* was inferred under
164 maximum parsimony, and the topology for *Avialae b* was inferred under Bayesian inference.
165 For Steell et al., two datasets were analysed with the same characters but slightly different
166 taxon samples and topologies (*Passeriformes a* and *Passeriformes b*). *Passeriformes a*
167 includes only extant taxa, and the topology was not inferred from the morphological matrix,
168 but from entirely independent molecular datasets from other studies (Prum et al. 2015;
169 Oliveros et al. 2019; Harvey et al. 2020). *Passeriformes b* includes all taxa from
170 *Passeriformes a* in addition to the fossil specimens analysed in the original publication, with
171 the topology inferred from the morphological dataset with a topological constraint for the
172 extant taxa based on the aforementioned molecular studies. Empirical topologies used in this
173 study are represented in Figure 1. The topologies used in this study were taken as previously
174 published; as such, some are unrooted and all except *Passeriformes a* are incompletely

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175 resolved (Fig. 1; Table 1). We chose to leave the trees in this condition instead of reanalysing
 176 them as we were interested in investigating patterns of homoplasy across a range of real
 177 datasets and phylogenetic trees, as opposed to reanalysing phylogenetic relationships.

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Dataset	Tree	Taxa	Chars.	Taxa: chars.	State # proportions (binary: 3: >3)	Supported nodes (%)	Missing data (%)
Telluraves ^a	MP	62	156	0.40	0.81:0.23:0.03	82.0	27.5
Passeriformes (a) ^b	-	142	49	2.90	0.86:0.14:0	100.0	7.5
Passeriformes (b) ^b	Bayesian	154	49	3.14	0.86:0.14:0	80.4	11.1
Neornithes ^c	Bayesian	39	295	0.13	0.67:0.28:0.04	89.5	18.4
Avialae (a) * ^d	MP	85	282	0.30	0.70:0.23:0.07	82.1	51.1
Avialae (b) * ^d	Bayesian	85	282	0.30	0.70:0.23:0.07	45.2	51.1

179 **Table 1 Summary of datasets.**

180 *No topological constraints applied in original phylogenetic analysis. Percentage of
 181 supported nodes is based on percentage of fully resolved nodes in the original publication of
 182 the phylogeny. ^a Ksepka et al. (2019); ^b Steell et al. (2023); ^c Field et al. 2020; ^d Benito et al.
 183 2022. Character numbers may differ from the original publication because invariant
 184 characters were removed prior to analyses in this work.

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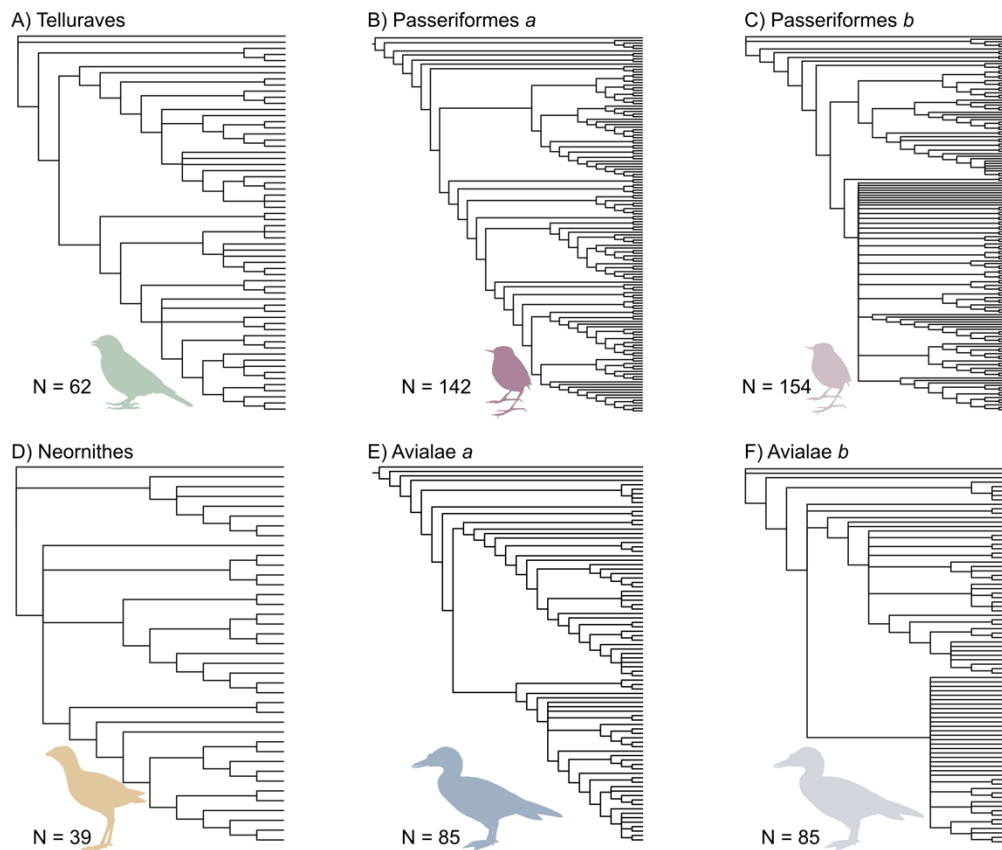


Figure 1 Phylogenetic trees without branch lengths used in analyses.

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All analyses were carried out in *R* v4.2.2 (R Core Team 2021), primarily using functions within the ‘APE’ (Paradis et al. 2004), ‘phangorn’ (Schliep 2011), and ‘dispRity’ (Guillerme 2018) packages. All code used here, including novel functions, can be found at github.com/LizzySteell/Homoplasy. Invariant characters were removed prior to analysis. Invariant characters are uninformative with respect to homoplasy, and removal was necessary because the RHI function requires the minimum number of states for any character to be two, rather than one. Inapplicable characters (usually represented as ‘-’) were treated as ambiguities (missing states; ‘?’) for simplicity. Using the ‘phyDat’ matrix format implemented in ‘phangorn’, we used contrast matrices to specify how steps should be counted for ambiguities and polymorphic scorings. Contrast matrices enable ambiguities (‘?’) to be interpreted as all possible numbered states (i.e., ‘0’, ‘1’, ‘2’, etc.), meaning no step is

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198 counted from a numbered state to an ambiguity and vice versa. Polymorphisms are
199 interpreted as all numbered states specified in the polymorphism (i.e., ‘{01}’ will be
200 interpreted as both ‘0’ and ‘1’). This means that when polymorphisms are present, the least
201 costly state in the polymorphism contributes to the tree length (for further discussion, see
202 Watanabe 2016). In this way, matrices in the ‘phyDat’ format implemented by ‘phangorn’
203 can be analysed with the same treatment of polymorphisms as in maximum parsimony
204 packages such as TNT (Goloboff et al. 2008). Therefore, all metrics calculated here represent
205 a *minimum* estimate of homoplasy, and increasing the proportion of ambiguities in a matrix
206 will further decrease the amount of homoplasy detected.

207 Consistency index and retention index were calculated for all empirical datasets with
208 all characters treated as unordered. CI and RI were calculated using CI() and RI() functions
209 from ‘phangorn’. For illustrative purposes CI and RI values are reported in the figures as 1 –
210 CI and 1 – RI, respectively, such that a value closer to 1 indicates more homoplasy than a
211 value closer to 0. This allows for a scale that is consistent across metrics and more easily
212 comparable. A new function was written to calculate the relative homoplasy index (RHI())
213 that includes the option to specify certain characters as ordered. The arguments for RHI() are
214 ‘data’ (matrix read into R using read.nexus()), ‘tree’ (phylogenetic tree of class ‘phylo’), ‘n’
215 (number of null trees to evaluate), ‘contrast’ (object containing a contrast matrix), ‘ord’ (a
216 vector specifying ordered characters; default = NULL) and ‘cost’ (object containing a cost
217 matrix to specify the number of steps taken during transitions of ordered character states;
218 default = NULL). To obtain a distribution of null tree lengths for RHI, tips were randomised
219 using sample() without replacement while maintaining the overall topology (tree shape). The
220 parsimony() function was then applied to the empirical matrix and each randomised tree to
221 obtain a distribution of values for L_{null} . Null tree length values are normally distributed
222 (Supplementary Figure 1, Appendix 1) but the range of values varies depending on the

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223 properties of the supplied tree and matrix. Generally, we recommend $n = 1000$; but $n = 100$
 224 may be adequate based on the simulations and the close similarity of the L_{null} distributions at
 225 different values of n (Supp. Fig. 1). The function outputs the median L_{null} , 5% and 95%
 226 quantiles, tree length (L) and theoretical minimum tree length (L_{min}). The second output in the
 227 list returned by RHI() is a vector containing the null tree lengths.

228 We carried out three analyses using simulated matrices based on empirical topologies,
 229 and three analyses with empirical topologies and associated empirical datasets. Analyses are
 230 summarised in Table 2.

231

Analysis	Datasets	Independent variable (X)	X values	Trees per run	Matrices per tree	Runs (# of X values)	Total iterations per run
<i>Simulated matrices</i>							
1. Inflating transition rate	Telluraves Passeriformes (a) Neornithes Avialae (a)	Mean of log transformed transition rate (μ)	-8 to 2 by 0.5	1	20	22	420
2. Varying number of taxa: sub-tree sampling	Telluraves Passeriformes (a)	Number of taxa	10 to 62 by 2 10 to 140 by 5	100	1	27	2700
3. Varying number of characters	Telluraves Passeriformes (a)	Number of characters	10 to 145 by 5 10 to 48 by 2	1	100	28	2800
<i>Empirical matrices</i>							
4. Comparison of	Telluraves Passeriformes (a)	na	na	na	na	1*	1000*

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homoplasy metrics across datasets	Passeriformes (b) Neornithes Avialae (a) Avialae (b)						
5. Varying number of taxa: sub-tree sampling	Telluraves Passeriformes (a) Passeriformes (b) Neornithes Avialae (a) Avialae (b)	Number of taxa	10 to 60 by 5 10 to 140 by 10 10 to 150 by 10 10 to 38 by 2 10 to 80 by 5 10 to 80 by 5	100	1	11 14 15 15 15 15	1100 1400 1500 1500 1500 1500
6. Varying number of characters: matrix sampling	Telluraves Passeriformes (a) Passeriformes (b) Neornithes Avialae (a) Avialae (b)	Number of characters	10 to 140 by 10 10 to 48 by 2 10 to 48 by 2 10 to 290 by 20 10 to 280 by 20 10 to 280 by 20	1	100	14 20 20 15 14 14	1400 2000 2000 1500 1400 1400

232 **Table 2 Summary of analyses.**

233 * 1 run per metric and 1,000 iterations (n = 1,000) for RHI only.

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235 *Investigating Homoplasy in Simulated Datasets*

236 Matrices were simulated with topologies following those in the source publications
237 (Fig. 1) for the six datasets (Table 1). These empirical topologies were selected as reference
238 trees for simulations with the aim of simulating realistic character matrices. Random tree
239 generation methods, such as the coalescent, birth-death or non-evolutionary model methods
240 implemented in ‘APE’ (Paradis et al. 2004) each produce trees with characteristic properties,
241 such as particular tree shapes, with different frequencies. Therefore, publication-derived
242 empirical topologies were used to avoid potential systematic bias resulting from random tree
243 generation methods. Estimating the extent of how homoplasy varies with respect to differing
244 tree shapes is beyond the scope of this study.

245 Matrix simulation required fully resolved (bifurcating) trees with branch lengths. We
246 used the accelerated transformation (ACCTRAN) algorithm (Farris 1970; Swofford and
247 Maddison 1987) as implemented in phangorn’s `acctran()` function with each empirical
248 topology and its corresponding empirical matrix to calculate and assign branch lengths. This
249 function also randomly resolves polytomies. Matrices were simulated using `sim.morpho()` in
250 the ‘DispRity’ package (Guillerme 2018). All simulations had a 9:1 binary to three-state
251 character distribution in the matrix, regardless of matrix dimensions. Matrices were simulated
252 under an equal rates Markov model (Lewis 2001) where rates among characters varied based
253 on a predefined lognormal distribution, and each transition within a character occurred at the
254 same rate with equal probabilities. A log-normal distribution was chosen as more appropriate
255 than a gamma distribution as morphological characters are likely affected by hierarchical
256 integration of characters (Wagner 2012). The standard deviation of the log-transformed rate
257 (`sd log`) was set to 0.5 in all simulations. The mean of the log-transformed rate (`mean log`)
258 was varied depending on the analysis (described below), as well as the number of simulations

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259 generated per run (Table 2). All metrics calculated for the simulated matrices assumed no
260 character state ordering. RHI for the simulations was performed for 100 iterations per run (n
261 = 100).

262 *Analysis 1: inflating transition rate*—I tested the sensitivity of RHI, CI and RI at
263 detecting homoplasy by using the transition rate of character state change as a proxy for
264 homoplasy in simulated matrices. Higher transition rates lead to increased homoplasy
265 because a greater number of character state transitions may result in independent acquisitions
266 or reversals to the same state (Simmons et al. 2004; Harrison and Larsson 2015). However,
267 the efficacy of increasing transition rates as a proxy for homoplasy will decrease with
268 increased numbers of character states present in a matrix. Moreover, the assumption of
269 homoplasy increasing in tandem with transition rates may not be valid if transitions between
270 states do not occur with equal probability. Therefore, the simulations assume a conservative
271 9:1 ratio of binary to three-state characters and equal probabilities of character state change
272 directionality. We varied transition rates by employing a range of values for the mean log (μ)
273 transition rate and simulating 20 matrices per rate category (Table 2). The range of values (-8
274 to 2) for μ was selected based on trialling multiple scenarios with different ranges of values;
275 this range of values was appropriate for the empirical datasets investigated here, as it covers
276 very low transition rates up to very high rates. The median, 5% and 95% quantiles of RHI, 1
277 – CI and 1 – RI were plotted against μ for four topologies (Table 3.2) which were chosen
278 based on their contrasting matrix dimensions. We also normalised median treelength between
279 0 and 1 with the following formula:

280 (7)
$$\frac{L - \min(L)}{\max(L) - \min(L)}$$

281 where $\min(L)$ and $\max(L)$ represent the minimum and maximum treelengths from the
282 simulation.

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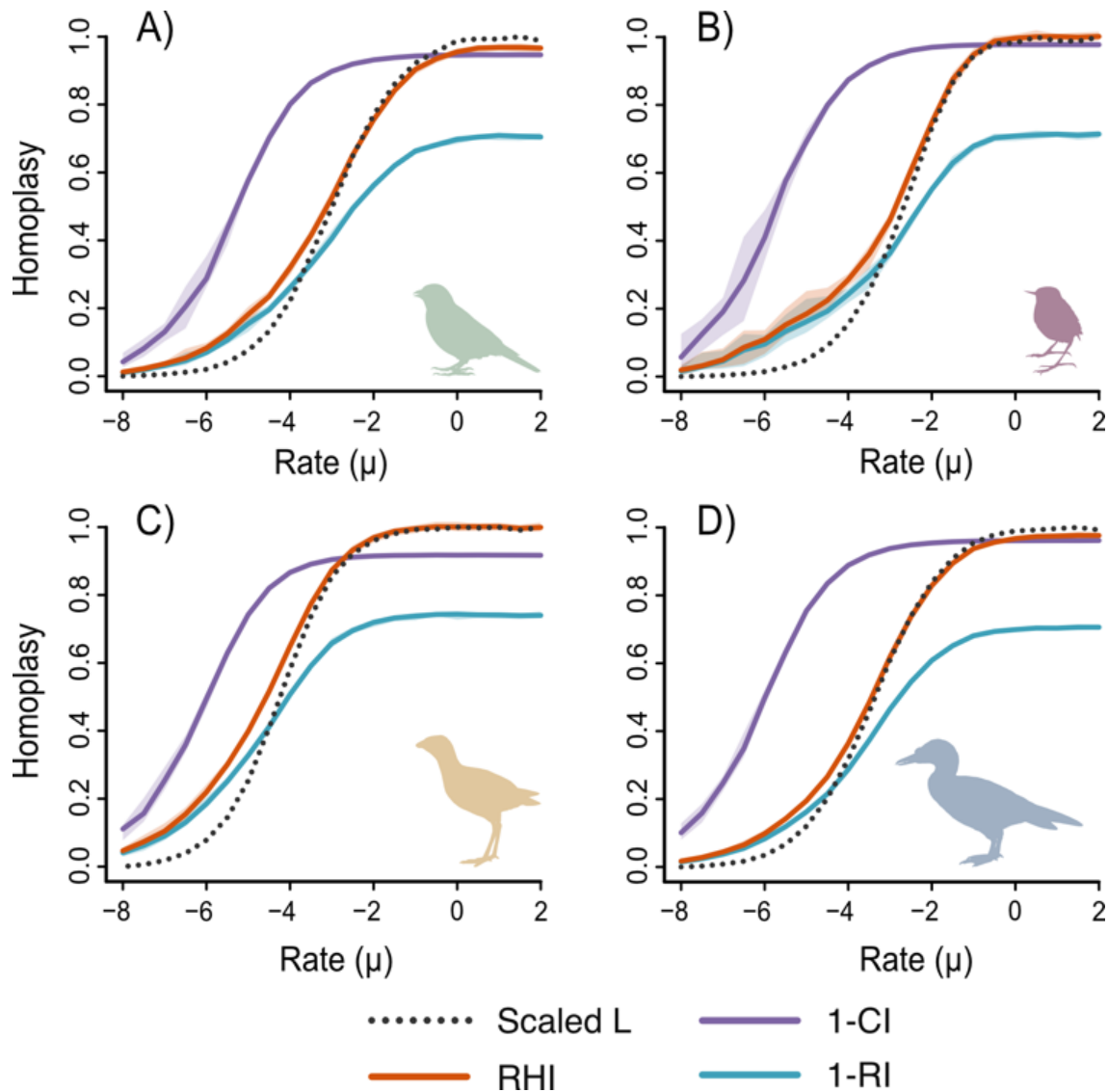


Figure 2 Results from Analysis 1: homoplasy inflation.

283 *Analysis 2: varying number of taxa with sub-tree sampling*—To test how homoplasy
 284 metrics behave with different numbers of taxa, we sampled sub-trees from two empirical
 285 topologies (Telluraves and Passeriformes *a*). A new function, `subset.trees()`, was written to
 286 sample sub-trees from a given topology (argument ‘tree’) where the number of tips to be
 287 retained (‘ntaxa’) and the number of samples to be taken (‘n’) are specified. One hundred
 288 sub-trees were sampled without replacement per set of taxa for each topology, with number
 289 of taxa decreasing in increments (Table 3.2). we investigated simulated matrices with two
 290 transition rate categories, $\mu = -5$ (slow rate) and $\mu = -3$ (fast rate). One matrix was simulated

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291 for each sub-tree. RHI, $1 - CI$ and $1 - RI$ were calculated for each simulated matrix and sub-
292 tree and plotted against number of taxa.

293 *Analysis 3: varying number of characters*—Similar to Analysis 2, we used the
294 topologies from Telluraves and Passeriformes *a* to investigate metrics with decreasing
295 numbers of characters. Number of characters was specified directly when simulating
296 matrices, and 100 matrices were simulated for each increment of character number, per
297 topology and rate category (Table 2). Rate categories were the same as for Analysis 2. For
298 both Analyses 2 and 3, we performed 20-30 runs per topology and rate category (Table 2).

299

300 *Homoplasy in Empirical Datasets*

301 *Analysis 4: comparison of homoplasy metrics across datasets*—RHI, CI and RI were
302 calculated for the six empirical datasets. Topologies were left as they were in the original tree
303 files; therefore, some topologies were not fully bifurcating, and some were unrooted (Fig. 1).
304 All metrics other than RHI were calculated with character states unordered, and RHI was
305 calculated with the set of ordered characters as specified in the original nexus file for each
306 dataset. RHI was run for 1,000 iterations ($n = 1,000$) per dataset, for both unordered and
307 ordered runs. The 5% and 95% quantiles for RHI were reported alongside the median value.

308 *Analyses 5 & 6: varying numbers of taxa and characters*—As in Analysis 2, number
309 of taxa was varied for Analysis 5 with sub-trees sampled from all six empirical topologies.
310 Metrics were calculated from the empirical matrices with each sub-tree. Number of
311 characters was varied for Analysis 6 by randomly sub-setting the empirical matrix without
312 replacement. All six datasets were investigated in Analyses 5 and 6. RHI calculations for
313 Analyses 5 and 6 assumed no character state ordering. Between 10–20 increments of
314 taxa/characters were analysed per dataset (Table 2).

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316 RESULTS

317 *Simulated Matrices*

318 Analysis 1 evaluated the sensitivity of each metric (RI, CI, and RHI) to increasing
319 character transition rates, a proxy for homoplasy. The results indicate that as transition rate
320 increases (by increasing mean log, μ), homoplasy increases (Fig. 2), although the extent of
321 homoplasy detected is dependent on the metric. Normalised tree length (scaled L) for each
322 dataset shows that at approximately $\mu = -2$, tree length reaches its maximum value for each
323 dataset (Fig. 2). The consistency index rapidly indicates more homoplasy with a small
324 increase in transition rate, and subsequently asymptotes at a much lower μ value than the
325 other metrics. In all datasets except Neornithes (Fig. 2c), $1 - CI$ reaches a maximum value of
326 1, with Neornithes reaching maximum value at 0.9. Retention index is more robust to
327 increases in transition rate, with $1 - RI$ reaching an asymptote at approximately equivalent μ

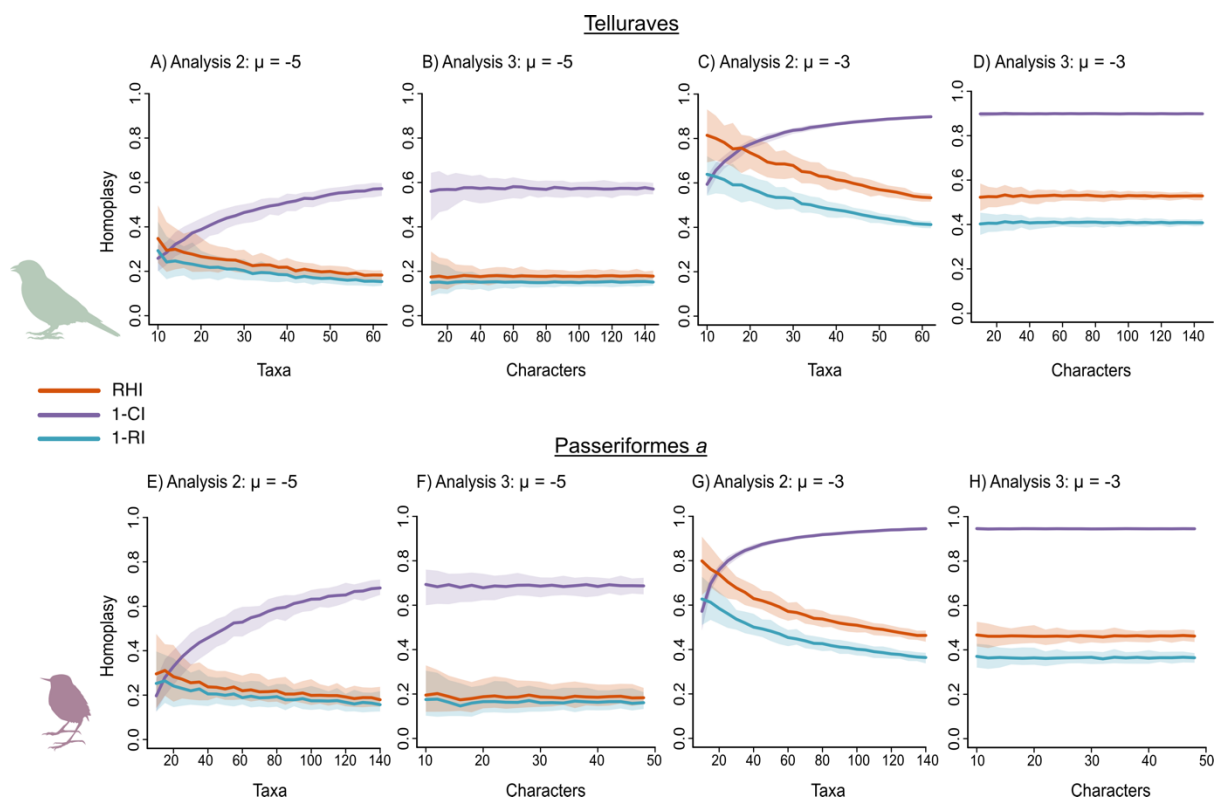


Figure 3 Results from Analyses 2 & 3: varying numbers of taxa and characters in simulated matrices.

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328 values to the asymptote point on the X axis of the normalised tree length. However, on the Y
 329 axis, $1 - RI$ does not occupy all homoplasy values between 0 and 1, and instead consistently
 330 asymptotes at values below 1. The relative homoplasy index follows the same general pattern
 331 as $1 - RI$ but occupies the full range of homoplasy values between 0 and 1 on the Y axis, and
 332 asymptotes at the same point on the X axis (equivalent μ values) as the normalised tree length
 333 in all datasets.

334 Analysis 2 tested the sensitivity of metrics to changes in number of taxa, while
 335 keeping number of characters the same. Across both low ($\mu = -5$) and high ($\mu = -3$) transition
 336 rates, Analysis 2 indicates that increasing the number of taxa in a topology impacts the
 337 homoplasy values estimated by CI, RI and RHI (Fig. 3a, c, e, g). Greater numbers of taxa
 338 cause increases in values of $1 - CI$, which asymptotes at a maximum value on the Y axis with
 339 fewer taxa at higher transition rates (Fig. 3c, g). In contrast, both $1 - RI$ and RHI values
 340 decrease as more taxa are added (Fig. 3a, c, e, g). The extent of decrease in the level of
 341 homoplasy detected by $1 - RI$ and RHI increases markedly at higher transition rates (Fig. 3c,
 342 g). In other words, if the character state transition rate is high, a greater decrease in
 343 homoplasy will be detected by RI and RHI when taxa are added into a dataset and all other
 344 variables stay the same. In Analysis 3, where the number of characters was varied but taxon
 345 number was held constant, there is no observable change across the investigated homoplasy
 346 metrics as the number of characters was increased (Fig. 3b, d, f, h). More variance was
 347 observed for each metric at lower numbers of both taxa and characters, as well as at lower
 348 transition rates (Fig. 3).

Dataset	Ordered characters			Unordered characters							
	<i>L</i>	RHI	5% & 95% quantiles	<i>L</i>	RHI	5% & 95% quantiles	RI	CI	1 - RI	1 - CI	

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Telluraves	714	0.45	0.4	0.4	702	0.45	0.4	0.4	0.6	0.2	0.40	0.74
			6	3			7	4	0	6		
Passeriformes	990	0.62	0.6	0.6	990	0.62	0.6	0.6	0.5	0.0	0.49	0.94
(a)			3	0			3	0	1	6		
Passeriformes	1056	0.62	0.6	0.6	1056	0.62	0.6	0.6	0.4	0.0	0.51	0.95
(b)			3	0			3	0	9	5		
Neornithes	1569	0.50	0.5	0.4	1498	0.50	0.5	0.4	0.5	0.2	0.42	0.73
			3	7			4	8	8	7		
Avialae (a)	1430	0.40	0.4	0.3	1407	0.41	0.4	0.4	0.6	0.2	0.35	0.72
			2	9			3	0	5	8		
Avialae (b)	1651	0.46	0.4	0.4	1616	0.47	0.4	0.4	0.5	0.2	0.42	0.76
			7	5			8	6	8	4		

349

Table 3 Summary of homoplasy metrics estimated for empirical datasets.

Estimates of homoplasy from each investigated method (consistency index, CI; retention index, RI; relative homoplasy index, RHI). *L*: tree length.

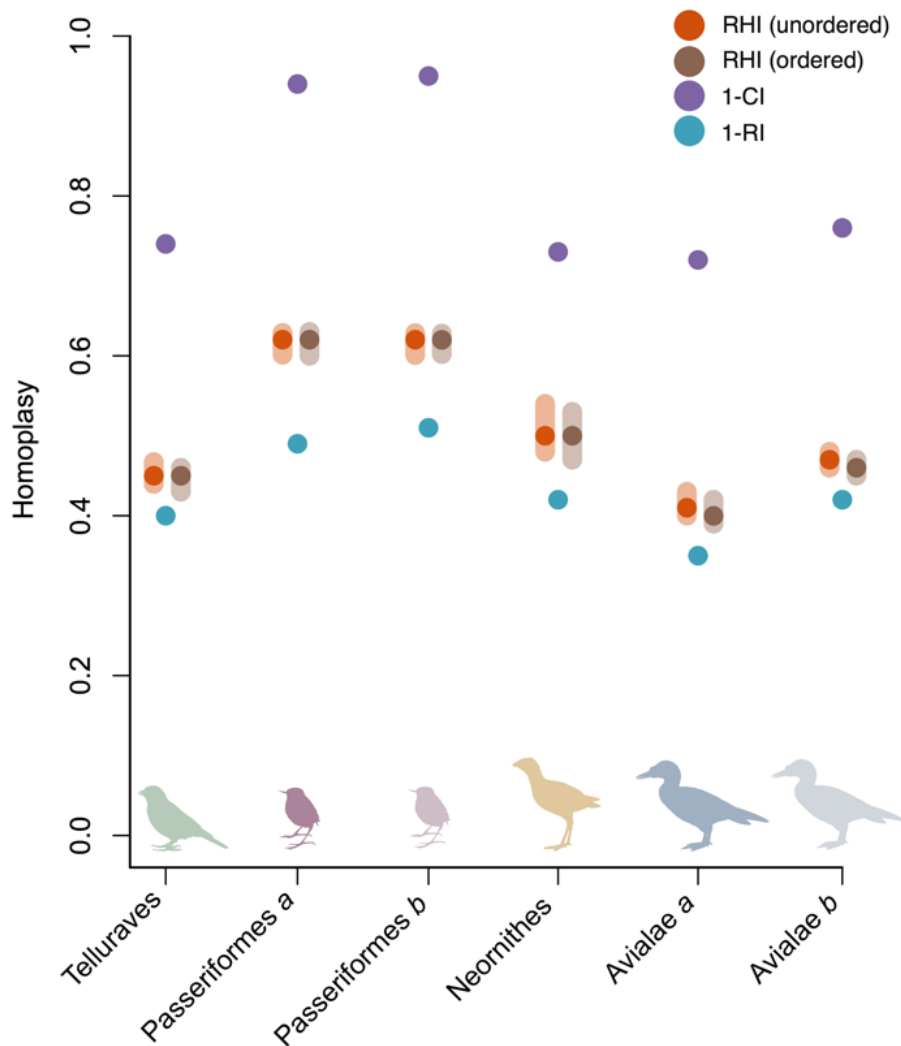


Figure 4 Results from Analysis 4: homoplasy levels in empirical datasets.

350

351 *Empirical Matrices*

352 In analysis 4, homoplasy was quantified with each metric for each empirical dataset,
353 and results are summarised in Table 3 and Figure 4. Overall, the two Passeriformes datasets
354 show the highest values for all metrics, across both ordered and unordered character
355 treatments, compared to the other bird matrices analysed here. For RHI, the 90% quantile
356 ranges overlap for ordered and unordered treatments for each dataset (Fig. 4). Neornithes
357 shows the greatest 90% quantile range, which is consistent with the comparatively shallow
358 bell curve of the Neornithes L_{null} distribution (Supplementary Figure 1, Appendix 1).

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359 Analyses 5 and 6 involved varying the number of taxa and characters, respectively, in
360 each empirical dataset through sampling. Analysis 5 also indicates that with increasing
361 numbers of taxa, 1 – CI increases, but 1 – RI and RHI decrease (Fig. 5a, c, e, g, i, k).
362 However, the manner in which values of 1 – CI, 1 – RI and RHI change with increasing the
363 size of the taxon samples varies depending on the empirical dataset investigated. Overall, 1 –
364 CI changes more abruptly than 1 – RI and RHI with increases in taxon sample, which
365 illustrate comparatively shallow decreases with additional taxa. Similar to Analysis 3,
366 Analysis 6 shows that increasing number of characters does not influence any of the
367 investigated homoplasY metrics (Fig. 5b, d, f, h, j, l).
368

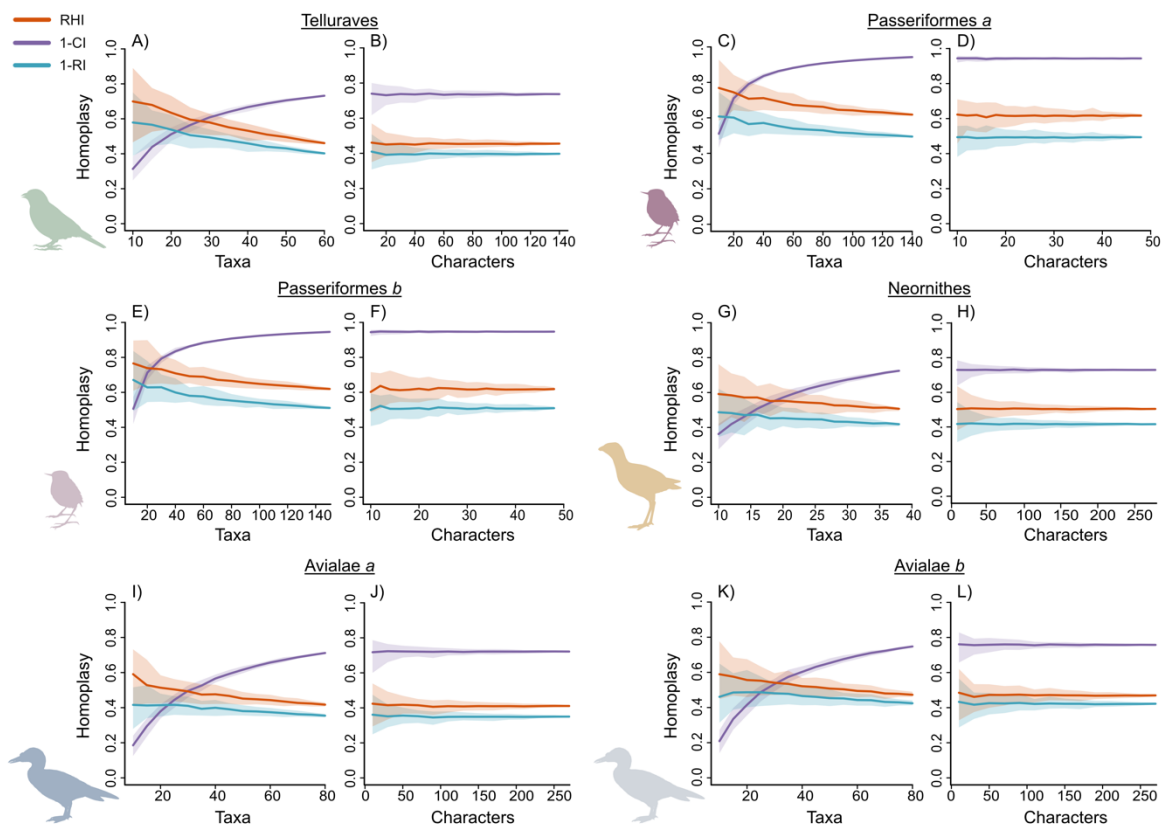


Figure 5 Results from Analyses 5 & 6: varying numbers of taxa and characters in empirical matrices.

369 DISCUSSION

370 Our new metric, the relative homoplasy index (RHI), uses a novel tip randomisation
371 approach to calculate the relative extent of homoplasy in a phylogenetic character-taxon
372 matrix by comparing the observed amount of homoplasy in that dataset to an estimated null
373 value for that matrix and topology. RHI is computationally tractable as implemented in the *R*
374 statistical environment (github.com/LizzySteell/Homoplasy) and provides better cross-
375 comparable estimates of homoplasy than the commonly used consistency index (CI) and
376 retention index (RI). Through analyses of both simulated and empirical discrete character
377 matrices, we show that RHI is more accurate at detecting homoplasy than CI and more
378 sensitive than RI, particularly in datasets with high levels of homoplasy.

379

380 *Patterns of Homoplasy*

381 Although RI has been considered robust with respect to variable numbers of taxa and
382 characters in phylogenetic datasets (Murphy et al. 2021), its major limitations are that it
383 underestimates the proportional extent of homoplasy in a given dataset, and cannot be
384 appropriately compared across alternative datasets because it is not scaled between zero and
385 one, but rather between zero and an arbitrary value conditioned on each particular dataset
386 (Archie 1996). As such, the main advantage of this newly proposed metric, the relative
387 homoplasy index (RHI) over RI is that values of RHI are scaled consistently (Fig. 2), and
388 therefore should provide a more useful method to accurately estimate the relative extent of
389 homoplasy in empirical datasets. The impact of this scaling consistency becomes particularly
390 important when datasets exhibit elevated levels of homoplasy; the simulations in Analysis 1
391 predict that matrices with greater overall transition rates, and therefore higher levels of
392 homoplasy, will show a greater divergence between $1 - RI$ and RHI values than matrices
393 with lower transition rates (Fig. 2). In other words, RI underestimates levels of homoplasy to
394 a greater extent in datasets exhibiting greater degrees of homoplasy. As expected, Analysis 4

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395 shows that the empirical matrices with the highest levels of homoplasy (Passeriformes *a* and
396 *b*) show a greater divergence between $1 - RI$ and RHI than the other datasets (Fig. 4). In
397 addition, RHI values are consistent across the alternative versions of the Passeriformes
398 dataset (Passeriformes *a* and *b*), but the RI values for each differ slightly (Table 3).

399 Analyses 2 and 5 show that homoplasy as estimated by RHI and RI decrease as taxon
400 numbers increase, whereas homoplasy detected by CI increases considerably with the
401 addition of taxa (Figs. 3 & 5; Table 2). This pattern in CI mirrors early work investigating
402 homoplasy in discrete matrices, which concluded that adding more taxa into a dataset would
403 increase estimated levels of homoplasy (Sanderson and Donoghue 1989). This longstanding
404 hypothesis has been corroborated by numerous subsequent studies (Meier et al. 1991; Hauser
405 and Boyajian 1997; Murphy et al. 2021), but the explanation of why homoplasy increases
406 with the addition of taxa has been somewhat simplistically attributed to the increased
407 detection of individual homoplastic character state changes with the addition of taxa and/or
408 characters (Sanderson and Donoghue 1989; Hauser and Boyajian 1997; Murphy et al. 2021).

409 CI decreases due to cumulative homoplastic events in a dataset resulting in a greater
410 tree length. However, when considering CI in this format:

$$411 \quad (8) \quad CI = \frac{L_{min}}{H + L_{min}}$$

412 H represents the number of extra steps for a tree with a given matrix, and can be considered
413 an unscaled, arbitrary value of homoplasy (Kluge and Farris 1969). L_{min} does not change with
414 respect to additional taxa, and only varies with changes in number of characters or the
415 composition of character states in a matrix. Therefore, although a tree has a greater
416 probability of gaining homoplastic state changes with the addition of more branches (i.e.,
417 increases in H via the addition of taxa), this raw quantification of homoplasy in the CI
418 equation is arbitrary and non-comparable; thus, the CI is not a useful tool when attempting to
419 compare estimates of homoplasy from alternative datasets. The original purpose of CI was to

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420 measure the consistency of a given dataset with a given tree in order to illustrate how far an
421 empirical topology diverged from a theoretical zero-homoplasy topology derived from a
422 version of the matrix where each character underwent the minimal number of changes (i.e., L
423 = L_{min} ; Kluge and Farris 1969; Farris 1989). The use of CI to quantify homoplasy has been
424 warned against previously due to its high sensitivity towards increasing numbers of taxa
425 (Archie 1989, 1996). We argue that CI should not be considered a measure of homoplasy at
426 all (after all, the opposite of ‘consistency’ as described above does not equate to homoplasy).
427 Rather, CI merely provides a proxy for homoplasy that performs poorly in the face of
428 variable taxon numbers—instead of directly tracking homoplasy, CI tracks an increase in tree
429 length that does not scale proportionally with changes in relative homoplasy.

430 RI and RHI, on the other hand, are expected to measure a decrease in homoplasy with
431 the addition of taxa to a given dataset, as demonstrated in our results (Figs. 3 & 5). The
432 addition of branches to a topology leads to an increase in the total potential amount of
433 homoplasy in a dataset (L_{max} in the case of RI and L_{null} in the case of RHI), due to the
434 exponentially increasing number of possible arrangements of tips as taxa are added
435 (Felsenstein 1978). However, provided the rate distribution of character state transitions for
436 the matrix is maintained, there is no reason to expect more homoplasy in a dataset with more
437 taxa. On the contrary, observed homoplasy values will be proportionally lower compared to
438 the increasing potential homoplasy of the dataset as a taxon sample grows in size.

439 We find that CI, RI and RHI do not vary with increasing numbers of characters (Figs.
440 3 & 5). For CI, provided the rate distribution of character state transitions is the same
441 regardless of number of characters, L and L_{min} (and therefore H) increase proportionally as
442 characters are added. For RI and RHI, again assuming transition rates are maintained, L and
443 L_{max} and L and L_{null} , respectively, also increase proportionally as characters are added.

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444 Previous studies investigating patterns of detected homoplasy with CI, RI and
445 additional parsimony metrics such as the homoplasy excess ratio (Archie 1989) and the
446 homoplasy slope ratio (Meier et al. 1991) report conflicting results. Archie (1989) observed
447 that RI (therein referred to as the ‘homoplasy excess ratio maximum’) detects less homoplasy
448 in subsets of datasets with more taxa, although a slight increase in homoplasy with the
449 addition of characters is observed (Archie 1989). Other studies using multiple non-subset
450 empirical datasets report mixed results regarding RI. For example, Hauser and Boyajian
451 (1997) found a slight decrease in homoplasy with increasing taxa in their meta-analysis of
452 600 datasets, but Murphy et al. (2021) showed the opposite trend in an analysis of 364
453 datasets. These variable patterns are likely explained by idiosyncrasies specific to the datasets
454 analysed; each dataset exhibits a particular amount of estimated homoplasy dependent on
455 factors such as tree shape, character state space (Simmons et al. 2004) and biological drivers
456 of homoplasy. As our results show, larger datasets do not show more homoplasy based on
457 their dimensions alone.

458

459 *Future Directions for Homoplasy Quantification*

460 Tree shape is expected to impact patterns of homoplasy estimation (Simmons et al.
461 2004), which is why a major advantage of the RHI is the tip randomising process. We
462 randomised tips to retain the overall tree shape of each empirical tree, rather than sampling
463 randomly generated trees that may come from a distribution of variable tree shapes with
464 unequal frequencies (Felsenstein 2004). Simmons et al. explored the effect of tree shape on
465 RI and CI with simulated datasets and found that with increasing transition rate, homoplasy
466 detected by RI is affected substantially depending on tree shape. At low transition rates,
467 levels of homoplasy increase significantly more for a completely asymmetrical, unequal
468 branch-length tree than they do for a completely symmetrical, equal branch-length tree

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469 (Simmons et al. 2004). Investigating homoplasy patterns with random trees generated by
470 different methods, for example those implemented in ‘APE’ (Paradis et al. 2004), was
471 beyond the scope of the current study but could be useful for the development of new, non-
472 parsimony methods for homoplasy quantification.

473 In the future, the RHI could be adapted and expanded to estimate homoplasy in a
474 probabilistic framework. Instead of counting steps directly from the matrix, branch-lengths
475 representing evolutionary change that are generated from statistical phylogenetic frameworks
476 (i.e., maximum likelihood or Bayesian inference) could be summed to estimate the observed
477 homoplasy in the dataset. However, randomising the tips would not be a sufficient method to
478 generate a null distribution of summed branch lengths because branch lengths remain the
479 same if the tree shape is retained. Therefore, an alternative way to simulate random trees in
480 order to estimate total potential homoplasy would be required. Statistical trait evolution
481 models, such as the birth-death model (Paradis 2010; Stadler 2011), could be utilised with
482 parameters modelled after the empirical topology to retain its characteristics. This would
483 open new avenues for estimating homoplasy beyond morphological datasets, and could
484 potentially be applicable to molecular sequence data.

485 The applications of quantifying homoplasy are far reaching. Homoplasy estimates can
486 be used to partition morphological datasets to improve phylogenetic resolution using per-
487 character homoplasy scores to place characters into rate categories (Rosa et al. 2019). It
488 would be possible to use a per-character application for RHI for this, although this step may
489 prove time-consuming. Using RI would likely be sufficient and faster for estimating levels of
490 homoplasy for individual characters in a matrix (for instance, by using the ‘sitewise’
491 argument in the RI() function in ‘phangorn’ (Schliep 2011)) in order to partition characters
492 into approximate categories. Nonetheless, for accurate estimates of per-character or whole
493 matrix homoplasy, RHI will perform better. Additionally, quantifying homoplasy enables the

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494 exploration of why clades are more morphologically labile or constrained. When
495 accompanied by methods investigating character state space and character state exhaustion
496 (Wagner 2000; Hoyal Cuthill 2015; Brocklehurst and Benson 2021), homoplasy
497 quantification can become a tool to better understand patterns in morphological
498 diversification and evolution (Sidlauskas 2008). The RHI metric provides an important
499 starting point in comparative analyses of homoplasy as it presents a non-computationally-
500 demanding method to directly compare the relative extent of homoplasy across empirical
501 phylogenetic datasets.

502

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513

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- 604

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605 FIGURE CAPTIONS

606

607 Figure 1 Phylogenetic trees without branch lengths used in analyses.

608 A) Unrooted, partially constrained topology of Telluraves from Ksepka et al. (2019); B)

609 Rooted, completely constrained topology of Passeriformes a (extant taxa only) from Steell et

610 al. (2023); C) Unrooted, partially constrained topology of Passeriformes b (extant and fossil

611 taxa) from Steell et al. (2023); D) Unrooted, partially constrained topology of Neornithes

612 from Field et al. (2020); E) Rooted, unconstrained Maximum Parsimony derived topology of

613 Avialae a from Benito et al. (2022); F) Unrooted, unconstrained Bayesian derived topology

614 of Avialae b from Benito et al. (2022).

615

616 Figure 2 Results from Analysis 1: homoplasy inflation.

617 Simulated matrices using empirical topologies with varying mean log of character state

618 transition rate (μ). Lighter coloured envelopes represent the 5% and 95% quantiles. A)

619 Telluraves topology; B) Passeriformes a topology; C) Neornithes topology; D) Avialae a

620 topology. Scaled L: Tree length normalised between 0 and 1; RHI: relative homoplasy index;

621 $1 - CI$: $1 -$ consistency index; $1 - RI$: $1 -$ retention index.

622

623 Figure 3 Results from Analyses 2 & 3: varying numbers of taxa and characters in simulated

624 matrices.

625 Simulated matrices using the empirical topologies of Telluraves (A–D) and Passeriformes a

626 (E–F) with varying numbers of taxa (A, C, E, G) and varying numbers of characters (B, D, F,

627 H) at two different mean log values of character state transition rate, slow ($\mu = -5$; A, B, E, F)

628 and fast ($\mu = -3$; C, D, G, H). Envelopes represent the 5% and 95% quantiles of each metric.

629 RHI: relative homoplasy index; $1 - CI$: $1 -$ consistency index; $1 - RI$: $1 -$ retention index.

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630 Figure 4 Results from Analysis 4: homoplasy levels in empirical datasets.
631 Summary of all metric results presented in Table 3 for each empirical dataset analysed in this
632 study. RHI envelopes represent 5% and 95% quantile ranges.
633
634 Figure 5 Results from Analyses 5 & 6: varying numbers of taxa and characters in empirical
635 matrices.
636 All empirical datasets with varying numbers of taxa (A, C, E, G, I, K) and varying numbers
637 of characters (B, D, F, H, J, L). Envelopes represent the 5% and 95% quantiles of each
638 metric.
639
640 Supplementary Figure 1 (Appendix 1) Kernel density plots of null tree length for each
641 empirical dataset.
642 Null tree length distributions during RHI estimation were visualised for different numbers of
643 null trees. Equivalent normal distributions for $n = 100, 1,000$ and $5,000$ suggest $1,000$ or even
644 100 null trees are sufficient to accurately estimate RHI. Kernel density plots were generated
645 using the base R function 'density()'.
646
647

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648 SUPPLEMENTARY MATERIAL

649 Data available from the Dryad Digital Repository: DOI: 10.5061/dryad.34tmpg4rp

650 R code and versions of code arising after this manuscript are available from

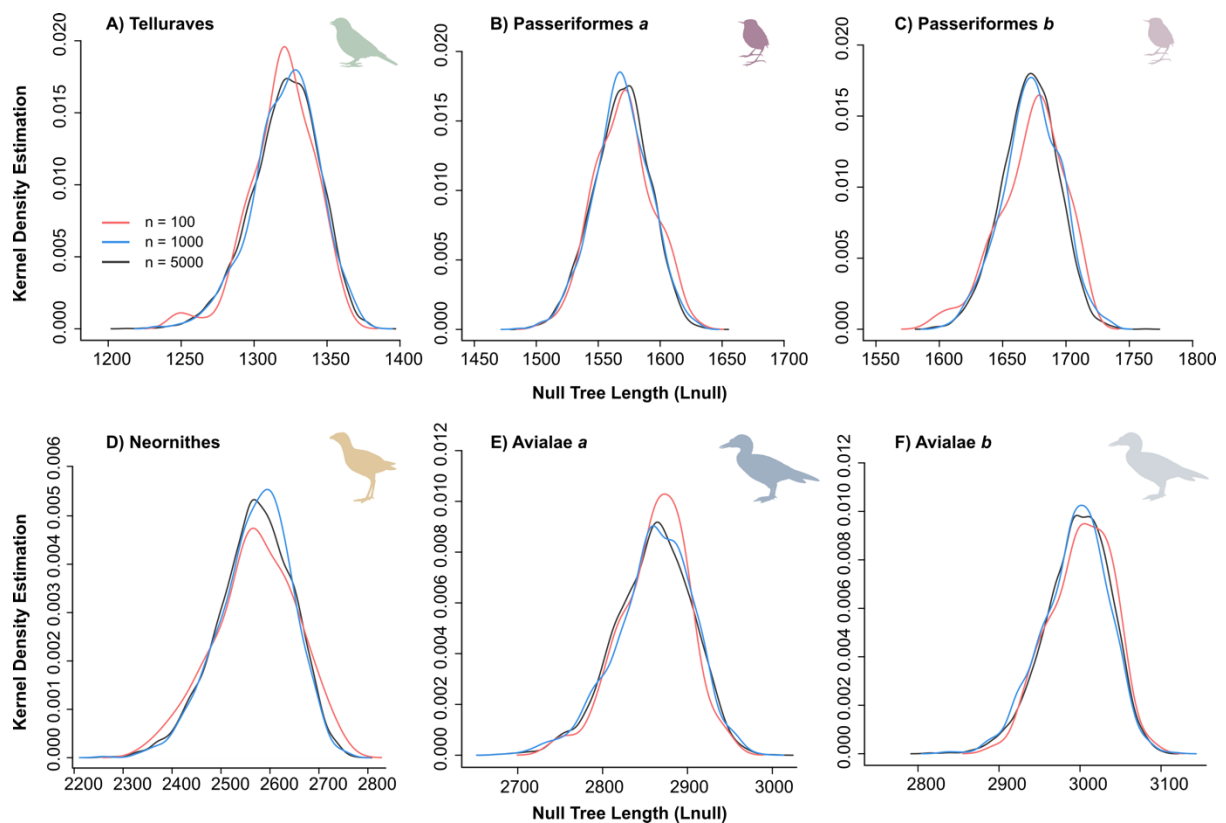
651 <https://github.com/LizzySteell/Homoplasy>

652

653 *Appendix 1*

654 *Investigating distribution of null tree lengths*

655



Supplementary Figure 1 Kernel density plots of null tree length for each empirical dataset.

656

657